

Context

What is inside a spherical satellite tank ?

- **Liquid ergol**: a perfectly wetting propellant,
- **Helium gas**: to pressurize the tank.

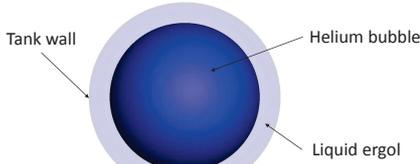


Figure 1. Inside a satellite tank

What is **ergol sloshing** ?

- Motion of fluids inside the tank which generates forces and torques on the tank wall and disrupts the stability of the satellite.

How to reduce ergol sloshing ?

- Add a thin hyperelastic membrane separating the ergol and the Helium
⇒ **Diaphragm tanks.**

Goal: Predict fluids and membrane behaviors inside the diaphragm tank.

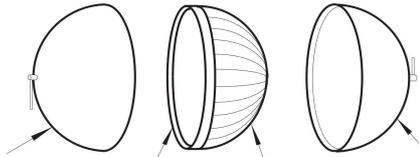


Figure 2. Exploded view of a diaphragm tank¹.

How to model sloshing ?

Experimental method: the **Fluidics** experiment.



Figure 3. The Fluidics experiment

- ⇒ CNES experiment sent to the ISS in 2017,
- ⇒ Sloshing measurement inside a simple tank.

Numerical method: the **monolithic approach**.

- ⇒ A single numerical code deals with the fluid and solid mechanics on a same mesh.

- ⇒ Numerical approach used in biomechanics, on deformation of biological cells.

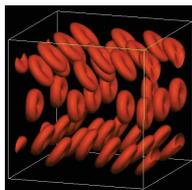


Figure 4. Numerical simulations of red blood cells in a flow².

Two-phase flow solver

Position of the two fluids with the **Level Set Method**, the signed distance from the interface:

Method, the signed distance from the interface:

- $$\begin{cases} \varphi > 0 : & \text{Presence of liquid ergol,} \\ \varphi = 0 : & \text{Interface between the two fluids,} \\ \varphi < 0 : & \text{Presence of Helium gas.} \end{cases}$$

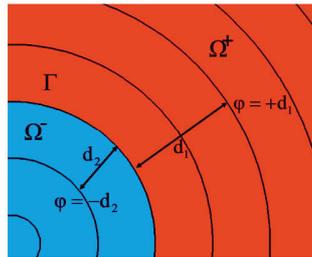


Figure 5. Level set scalar field.

Irregular domain method for the spherical tank wall:

- Second level set function φ_S for the interface between the tank wall and the fluids,
- Specific boundary conditions.

Two-phase flow solver:

- Solve the Navier-Stokes equations,
- Consider the jump conditions on the viscosity and density.

Eulerian membrane model

Some definitions:

- A hyperelastic behavior is an elastic behavior even for large strains.
- The zero level set of φ corresponds to the position of the thin membrane in the domain.

Membrane model algorithm²:

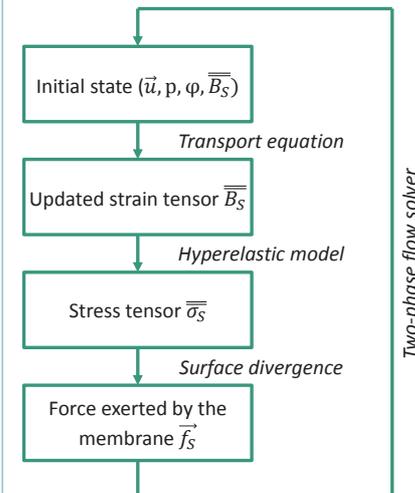


Chart 1. Implemented algorithm of the membrane model.

Validation on test cases

2D stretched pressurized membrane³:

- Material model : linear Hooke law,
- Same fluid inside and outside the membrane,
- Computational domain : closed box.

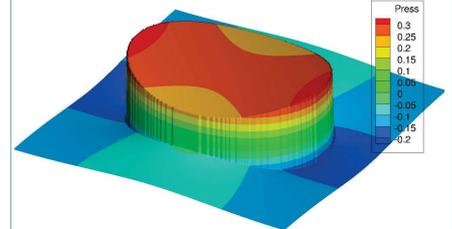


Figure 6. Pressure jump at the membrane.

⇒ Relaxation or oscillation of the membrane around its equilibrium position depending on the Reynolds number.

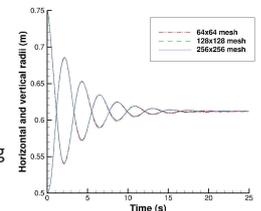


Figure 7. Radii evolution of the 2D membrane for a high Reynolds number.

3D capsule immersed in a shear flow⁴:

- Spherical membrane at rest,
- Material model : Neo-Hookean law,
- Same fluid inside and outside the capsule.

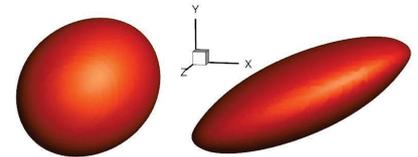


Figure 8. Two deformed surfaces of the capsule.

⇒ Elongation of the capsule depending on the ratio between the fluid viscosity and the membrane elasticity G .

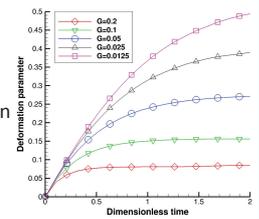


Figure 9. Evolution of the deformation parameter of the 3D capsule.

Conclusions

- Numerical model of the fluids and membrane behaviors using a monolithic approach.
- Solver based on a two-phase flow solver upgraded with an eulerian membrane model.
- Validation on classical membrane test cases by comparing with literature results.

Perspectives:

- Different fluids inside/outside the membrane,
- Contact of the membrane with a wall,
- Simulation of a real diaphragm tank.

References

1. I. A. Ballinger, W. D. Lay and W. H. Tam, 1995, Review and History of PSI Elastomeric Diaphragm Tanks, AIAA 95-2534.
2. S. li, X. Gong, K. Sugiyama, J. Wu, H. Huang and S. Takagi., 2012, A full eulerian fluid-membrane coupling method with a smoothed volume-of-fluid approach. *Comm. Comput. Phys.* **12**, 544-576.
3. L. Lee and R. J. Leveque, 2003, An immersed interface method for incompressible Navier-Stokes equations. *J. Sci. Comput.* **25**, 832-856.
4. C. Pozrikidis, 1995, Finite deformation of liquid capsules enclosed by elastic membranes in simple shear flow, *J. Fluid Mech.* **297**, 123-152.